

Physics 106b: Electrodynamics

Problem Set I

Due: 4pm, Friday, February 20, 2009

Remember: Late homework will be granted 50% credit up to one week late, unless you have a note from the Dean or a health official. Homework should be turned into the box outside 114 Sloan Annex.

Reading: Griffiths Chapter 2

Problems:

1. Prove $\nabla \times (\mathbf{A} \times \mathbf{B}) = (\mathbf{B} \cdot \nabla) \mathbf{A} - (\mathbf{A} \cdot \nabla) \mathbf{B} + \mathbf{A}(\nabla \cdot \mathbf{B}) - \mathbf{B}(\nabla \cdot \mathbf{A})$ using ε_{ijk} and the repeated index summation convention. Recall that $\varepsilon_{ijk} \varepsilon_{klm} = \delta_{il} \delta_{jm} - \delta_{im} \delta_{jl}$
2. Griffiths 2.33
3. Griffiths 2.36
4. Griffiths 2.41
5. Evaluate numerically (to 3 significant figures), the delta-function integral

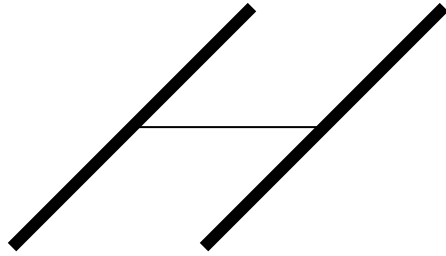
$$\int_0^{\pi} \frac{\delta(J_0(x))}{(x+1)^2} dx$$

$J_0(x)$ is the zeroth order ordinary Bessel function. Explain all steps; do not hand in the output of some symbolic math program like *Mathematica*. You may however use tabulated values of $J_0(x)$.

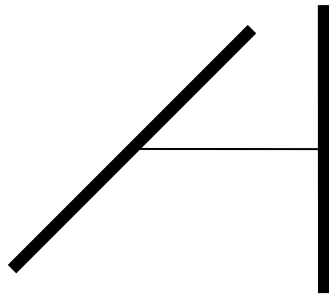
6. Consider two thin rods, each of length L . One rod carries a uniform linear charge density λ , while the other is uniformly charged with density λ' . These rods are attached, at their middles, to opposite ends of a third rod of length H . This third rod is uncharged. Assume that the charged rods are both perpendicular to the axis of the shorter rod.
 - a) Calculate the force on each charged rod assuming they are parallel to one another.
 - b) Do the same, but now with the charged rods perpendicular to one another. (It's helpful to check that your results make sense when $H \gg L$)

-SEE NEXT PAGE-

These (poor) diagrams suggest the arrangements



charged rods parallel



charged rods perpendicular